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Josep J. Centelles 
Universitat de Barcelona, Spain

Estefania Moreno 
Universitat de Barcelona, Spain

Pedro R. de Atauri 
Universitat de Barcelona, Spain

Santiago Imperial 
Universitat de Barcelona, Spain

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Problem-Based Learning for Calculating Kinetic Parameters from Michaelis-Menten Equation

Josep J. Centelles, Estefania Moreno, Pedro R. de Atauri, Santiago Imperial

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Abstract

In “Advanced Enzymology” at the University of Barcelona, we teach various methods for identifying uni-uni irreversible reactions. Kinetic constants such as maximum velocity (V_{max}) and Michaelis constant (K_m) are calculated using non-linear regression with the Michaelis-Menten equation. However, if a computer is not available, students must calculate these kinetic parameters using linear regressions with Lineweaver-Burk, Eadie-Hofstee, and Hanes-Woolf plots. Michaelis-Menten equation: $v = (V_{max} [S]) / (K_m + [S])$, Lineweaver-Burk equation: $1/v = (K_m/V_{max}) (1/[S]) + 1/V_{max}$, Eadie-Hofstee equation: $v = -K_m (v/[S]) + V_{max}$, Hanes-Woolf equation: $[S]/v = (1/V_{max}) [S] + (K_m/V_{max})$. The objective of this work was that students explore various methods for calculating kinetic constants and determine the most effective approach. A problem was prepared with data on substrate concentrations ($[S]$) and reaction rates (v). Data points with lower substrate concentration, and also with lower velocities had higher errors. The Michaelis-Menten plot provided only an approximate estimation of the kinetic constants, as it is not a linear graph. The Lineweaver-Burk plot generated maximum velocities that were too low due to the higher errors for low substrate concentrations, rendering impossible values of the kinetic parameters. The Eadie-Hofstee plot provided better results, as the values of $v/[S]$ compensated their errors. Furthermore, kinetic constants were obtained directly from the slope and intersection of the line equation. The Hanes-Woolf plot also produced correct values for kinetic parameters, since high substrate concentrations were less erroneous than lower ones. After completing this computer class, students were very satisfied and learned the different methods for obtaining kinetic parameters. Non-linear regression is undoubtedly the most accurate method for obtaining kinetic parameters values. However, in the absence of computers, the Eadie-Hofstee plot is the best and most commonly used plot in kinetic papers.

Introduction

Despite the difficulties of their time, Maud Menten (1879-1960), a woman, and Leonor Michaelis (1875-1949), a German-Jewish man, managed to develop in 1913 a well-known equation in enzyme kinetics [López-Nicolás and García-Carmona, 2015]. The paper published in 1913 is one of the most cited in Biochemistry journals. The

Michaelis-Menten equation describes the relationship between the rate of an enzyme-catalyzed reaction and the concentration of the substrate. The equation is expressed as:

$$v = (V_{\max} [S]) / (K_m + [S])$$

where v is the rate of the reaction, V_{\max} is the maximum rate of the reaction, $[S]$ is the concentration of the substrate and K_m is the Michaelis constant [Michaelis and Menten, 1913]. To find the values of the kinetic parameters (V_{\max} and K_m) from the Michaelis-Menten equation, a series of experiments is usually carried out in which the reaction rate is measured at several substrate concentrations, keeping constant all the other variables (temperature, pH, ion concentrations, ...). Data obtained from these experiments can be represented graphically, with the reaction rate (v) on the vertical axis and the substrate concentration ($[S]$) on the horizontal axis. The resulting curve is known as the Michaelis-Menten curve, and it is a hyperbolic function.

Non-Linear Regression

Once the Michaelis-Menten curve has been obtained, the kinetic parameters can be calculated by fitting the curve to the Michaelis-Menten equation using non-linear regression analysis. This involves finding the best values of V_{\max} and K_m that minimize the difference between the observed reaction rates and the predicted values calculated using the Michaelis-Menten equation. However, at the beginning of the 20th century, it was not yet known how to perform non-linear regressions, and the kinetic parameters were determined in an approximate way. To do this, an approximate asymptote to the Michaelis curve (V_{\max}) was sought and the substrate concentration that generated a velocity equal to half the maximum velocity (K_m) was calculated. Starting from the equation, various authors searched for other methods to calculate the kinetic parameters, using several linearizations. Currently, the linearization methods of the Michaelis-Menten equation are alternative methods to obtain the kinetic parameters of the enzyme from the experimental data and allow to determine V_{\max} and K_m by linear regression.

Lineweaver-Burk linearization

Hans Lineweaver (1907-2009) and Dean Burk (1904-1988) published in 1934 a method to calculate the kinetic parameters of the Michaelis-Menten equation, by means of a transformation of the equation. This mathematical transformation is the most commonly used, and consists of the reversion of the Michaelis-Menten equation, which results in the linear Lineweaver-Burk equation [Lineweaver-Burk, 1934]:

$$1/v = (K_m/V_{\max})(1/[S]) + 1/V_{\max}$$

where $1/v$ is the reverse of the reaction rate, $1/[S]$ is the reverse of the substrate concentration, K_m is the Michaelis constant, and V_{\max} is the maximum velocity of the reaction. The Lineweaver-Burk equation is represented graphically as a straight line with $1/v$ on the vertical axis and $1/[S]$ on the horizontal axis. For this reason, the Lineweaver-Burk representation is also called the double reciprocal representation. The slope of the line is equal to K_m/V_{\max} , while the intersection is equal to $1/V_{\max}$. To obtain the values of K_m and V_{\max} from the linear

Lineweaver-Burk equation, a linear regression analysis is performed to fit the experimental data to a straight line. From the slope and intersection obtained from the straight line, the values of K_m and V_{max} can be calculated using the following equations:

$$K_m = (\text{slope of the line}) / (\text{intersection})$$

$$V_{max} = 1 / (\text{intersection})$$

Eadie-Hofstee Linearization

Related on an earlier work performed by Augustinsson [1948], Hofstee devised another linearization to identify the kinetic parameters [Hofstee, 1952]. The corresponding plot is called the Woolf-Augustinsson-Hofstee plot and it is obtained from the Lineweaver-Burk linearization by multiplying both sides of the equation by $v \cdot V_{max}$:

$$V_{max} = K_m (v/[S]) + v$$

$$v/[S] = - (1/K_m) \cdot v + V_{max}/K_m$$

The representation of this equation is obtained by placing $v/[S]$ on the vertical axis and v on the horizontal axis. A straight line is obtained with a slope of $-1/K_m$ and an intersection of V_{max}/K_m .

$$K_m = - 1/ (\text{slope of the straight line})$$

$$V_{max} = (\text{intersection}) / - (\text{slope of the straight line})$$

Nevertheless, a modification on the previous graph, presented by George Sharp Eadie (1895-1976) in a 1942 publication [Eadie, 1942], consists in exchanging the axes of the Woolf-Augustinsson-Hofstee plot. This variation (Eadie-Scatchard-Hofstee graph) directly generates the kinetic parameters from the intersection and the slope:

$$v = - K_m (v/[S]) + V_{max}$$

In this case, v is represented on the vertical axis and $v/[S]$ on the horizontal axis, that is, the axes of the previous graph are inverted. A straight line is obtained with a slope of $- K_m$ and an intersection of V_{max} .

$$K_m = - (\text{slope of the straight line})$$

$$V_{max} = (\text{intersection})$$

Although in this second case the kinetic parameters are obtained directly from the equation of the line and it seems better than the previous one, there is not much difference between the two previous graphs. Both graphs receive different names from the authors who developed them (Eadie-Hofstee graph, Woolf-Eadie-Augustinsson graph or Eadie-Augustinsson graph) [Segel, 1979], and it is not very clear if the representation consists of $v/[S]$ vs. v or v vs. $v/[S]$.

Hanes-Woolf Linearization

Charles Samuel Hanes (1903-1990) performed another transformation of the Michaelis equation [Hanes, 1932] to calculate the kinetic parameters. The Hanes-Woolf mathematical transformation is generated by multiplying the Lineweaver-Burk equation by [S], obtaining the expression:

$$[S]/v = (K_m/V_{max}) + (1/V_{max}) [S]$$

To linearize this equation, a plot using [S]/v on the vertical axis and [S] on the horizontal axis is performed. A straight line is obtained with a slope of 1/V_{max} and an intersection of K_m/V_{max}.

$$V_{max} = 1/(\text{slope of the straight line})$$

$$K_m = (\text{intersection}) / (\text{slope of the straight line}).$$

Method

In this study we used a problem-based learning so that the students of the subject "Advanced Enzymology" could:

- Identify the data for the Michaelis-Menten equation and calculate the kinetic parameters from the data and the graph.
- Plot the Lineweaver-Burk linearization and calculate the kinetic parameters obtained from this plot.
- Analyze the errors of the Lineweaver-Burk plot.
- Plot the Eadie-Hofstee linearization and calculate the kinetic parameters obtained from this plot.
- Plot the Hanes-Woolf linearization and calculate the kinetic parameters obtained from this plot.
- Calculate the kinetic parameters by using non-linear regression.
- Compare the kinetic parameters obtained by the various methods and identify which is the best plot to calculate the most accurate kinetic parameters by linear regression.

Problem-based learning is an educational methodology that focuses on active learning and on problems solving rather than memorizing information. In problem-based learning, students work in small groups to discuss complex, realistic problems. The objective of this method is to develop critical thinking and problem-solving skills, as well as to encourage teamwork and collaboration. The problem-based learning process generally consists of the following steps:

- Problem identification: Students handle a complex and realistic problem that must be solved.
- Problem definition: Students identify the components of the problem and determine what is known and what is unknown.
- Investigation: Students carry out an investigation to gather relevant information about the problem.
- Analysis and synthesis: Students analyze and synthesize the information collected to develop solutions to the problem.

- Presentation: Students present their solutions and discuss their findings with the group.
- Reflection: Students discuss on the solved problem and the learning acquired.

This methodology is considered as an active method and very effective promoting information retention, improving students' motivation and self-efficacy, and developing practical and applicable skills in the real world. An active learning is much better when students face with situations that require the practical application of what they have learned theoretically. Rather than simply memorizing information, students must use what they know to solve complex problems and situations in a simulated or real environment. Problem-based learning also promotes collaboration and teamwork.

Students work in small groups to discuss problems, which allows them to learn not only from their own experience, but also from the experience of their partners. Teamwork also helps students to develop interpersonal skills, such as effective communication and conflict resolution. In addition, this method encourages reflection on the learning process and problem solving. By reflecting on their experience, students can identify what worked well and what didn't, allowing them to simplify their future problems. In our case, problem-based learning is based on solving a proposed problem in the computer room, so that student can also use a web page that calculates the kinetic parameters by non-linear regression.

Each student has a computer to be able to personally use the Excel program and to be able to make the representations and to calculate the kinetic parameters for each linearization method. However, students will be able to discuss among themselves, and the results will be discussed during the class. By using this methodology, students can develop practical and applicable skills in the real world, as well as encourage collaboration and reflection on the learning process.

Proposed Problem

To calculate the kinetic parameters of an enzyme, activity determinations were performed by always adding a fixed amount of enzyme to a series of reaction mixtures containing different concentrations of substrate ($[S]$). The other conditions were kept constant (pH, temperature, ionic strength, ...). From the slope of the straight line in the initial phase of the progress curve, the initial velocity values shown in Table 1 were calculated and obtained:

From these results, calculate the values of V_{max} and K_m of the enzyme, considering that the enzyme is Michaelian. Calculate the kinetic parameters by using the following methods:

- a) Looking the data (or from the Michaelis-Menten plot).
- b) From the Lineweaver-Burk plot using linear regression.
- c) From the Eadie-Hofstee plot using linear regression.
- d) From the Hanes-Woolf plot using linear regression.
- e) Using a non-linear regression method.

Table 1. Data of Substrate Concentrations [S] and Initial Velocities (v).

[S] (μM)	v ($\mu\text{mol/L min}$)
0.2	0.81
4.0	15
20.0	60
40.0	120
80.0	192
120.0	240
200.0	300
400.0	360
2000.0	450
4000.0	465

Results

Calculation of the Kinetic Parameters from Data (or from Michaelis-Menten Plot)

Students are expected to identify that the maximum velocity value presented in Table 1 is $465 \mu\text{mol/L min}$. Thus, the maximum velocity of the enzyme must be greater than or equal to this value. One possibility is to choose a maximum velocity value of $V_{\text{max}} = 480 \mu\text{mol/L min}$. Since the value of K_m can be defined as the substrate concentration showing a reaction rate equal to half the maximum velocity, the student must find $V_{\text{max}}/2$ ($480 \mu\text{mol/L min}/2 = 240 \mu\text{mol/L min}$). As it can be seen in Table 1, a velocity of $240 \mu\text{mol/L min}$ corresponds to the substrate concentration $[S] = 120 \mu\text{M}$. Thus, $K_m = 120 \mu\text{M}$. Similarly, it is possible to perform the Michaelis plot (v versus [S]) using the Microsoft Office Excel program (or a similar data processing program), obtaining the plot of Figure 1.

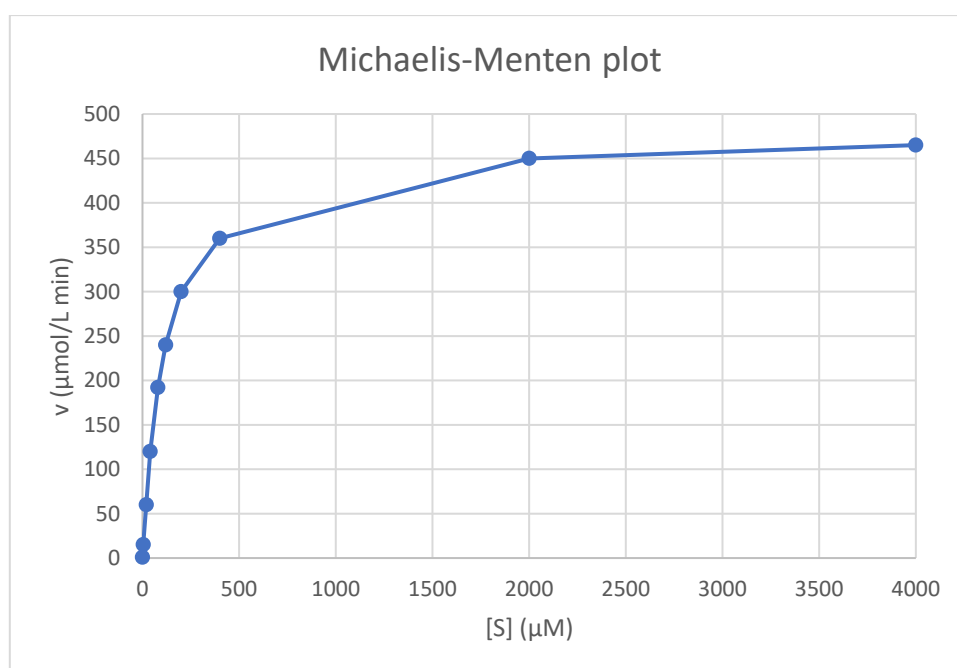


Figure 1. Michaelis-Menten plot (v vs. [S])

If a value of $V_{max} = 500 \mu\text{mol/L min}$ is taken, the value of $V_{max}/2 = 250 \mu\text{mol/L min}$ lies between the values of $[S] = 120 \mu\text{M}$ ($v = 240 \mu\text{mol/L min}$) and $[S] = 200 \mu\text{M}$ ($v = 300 \mu\text{mol/L min}$). By interpolation, it is possible to calculate $\Delta[S] = 200 - 120 = 80$, which is equivalent to $\Delta v = 300 - 240 = 60$. If $V_{max}/2 = 250$ ($\Delta v = 300 - 250 = 50$). Interpolation indicates that $\Delta[S] = 80 \cdot 50/60 = 66.67$. From this data, $[S]_{50} = K_m = 200 - 66.67 = 133.33 \mu\text{M}$. Depending on the value of V_{max} used, different K_m values will be obtained ($V_{max} = 480 \mu\text{mol/L min}$, $K_m = 120 \mu\text{M}$; $V_{max} = 500 \mu\text{mol/L min}$, $K_m = 133.33 \mu\text{M}$). Thus, this method is not very confident.

Calculation of the Kinetic Parameters from Lineweaver-Burk Plot Using Linear Regression

A linear regression can generate more reliable kinetic parameters values than an approximate calculation such as the one made by directly using the Michaelis-Menten equation. The Lineweaver-Burk or double reciprocal plot focuses on reversing the Michaelis-Menten equation. Reversion of the Michaelis-Menten equation gives the Lineweaver-Burk equation:

$$1/v = (K_m/V_{max}) (1/[S]) + (1/V_{max})$$

The representation of $(1/v)$ versus $(1/[S])$ shows a line, and from the linear regression, the slope of the line will be (K_m/V_{max}) and the intersection $(1/V_{max})$. Figure 2 shows the Lineweaver-Burk plot, using all the points of the proposed problem.

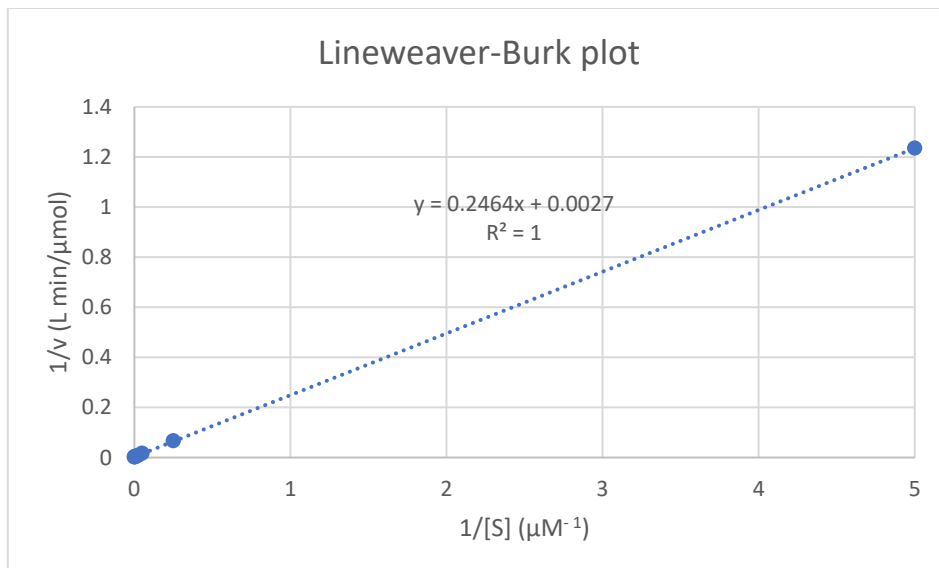


Figure 2. Lineweaver-Burk plot ($1/v$ Versus $1/[S]$). This Plot Shows All the Data for the Problem.

The plot of all the data of the problem allows to calculate, from the linear regression, the following values for the kinetic parameters: $V_{max} = 1/0.0027 = 370.37 \mu\text{mol/L min}$ and $K_m = 0.2464/0.0027 = 91.26 \mu\text{M}$. It is observed that the V_{max} is lower than some of the velocity values obtained at $[S]$ of $2000 \mu\text{M}$ and $4000 \mu\text{M}$. The calculated value of V_{max} is therefore not real. The student must also observe that, although $R^2 = 1$, the equation of the line is not correct. The points are not correctly distributed along the line, as the plot shows one single point at one end of the line and an accumulation of points at the other end of the line. Since a line always goes through two points,

it appears that the line seems correct (with $R^2 = 1$), but it is not. It must be considered that when $[S]$ is very low, the error both in the preparation of the substrate concentration and in the determination of the reaction rate, which will also be low, will be much higher than if the $[S]$ is higher. In Figure 2, a lot of weight is given to $[S] = 0.2 \mu\text{M}$, and if its velocity is wrong, the calculation of the kinetic parameters will also be wrong. Logic indicates that this point, corresponding to a low $[S]$ and a low velocity, should be removed. Figure 3 shows the Lineweaver-Burk plot when the point corresponding to $[S] = 0.2 \mu\text{M}$ and $v = 0.81 \mu\text{mol/L min}$ has been removed.

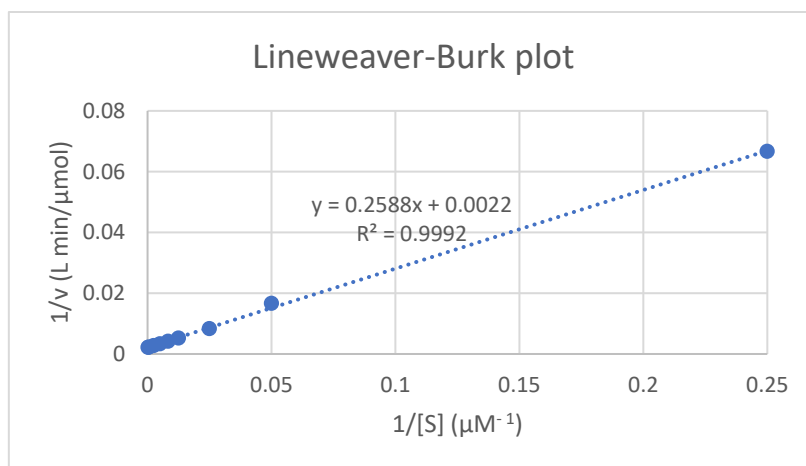


Figure 3. Lineweaver-Burk plot ($1/v$) versus ($1/[S]$). In This Graph, the point (5, 1.23) Has Been Removed. This Point Corresponds to (0.2, 0.81), the Lower $[S]$ and Lower v .

In Figure 3, the last point is still quite separate from the others. In this case, the following kinetic parameters are obtained: $V_{\text{max}} = 1/0.0022 = 454.54 \mu\text{mol/L min}$ and $K_m = 0.2588/0.0022 = 117.64 \mu\text{M}$. The value of $V_{\text{max}} = 454.54 \mu\text{mol/L min}$ is still lower than the rate of $[S] = 4000 \mu\text{M}$, although the value is close and could be an experimental error. However, we can proceed by removing the second point, corresponding to $[S] = 4.0 \mu\text{M}$. In this case, Figure 4 is obtained.

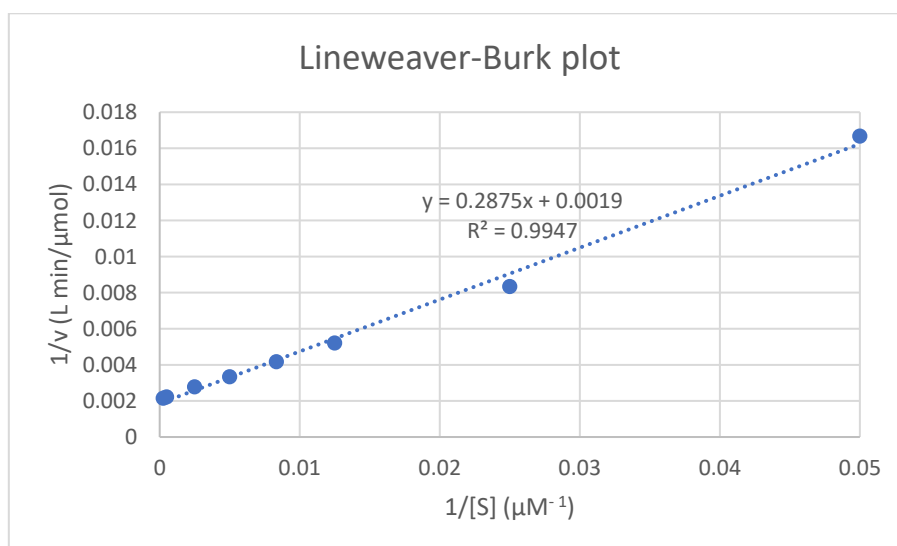


Figure 4. Lineweaver-Burk Plot ($1/v$) Versus ($1/[S]$). In This Graph, the Points (5, 1.23), (0.25, 0.067) Have Been Removed. These Points Correspond to (0.2, 0.81), (4.0, 15), the Lower $[S]$ and Lower v .

The kinetic parameters calculated by removing two points were: $V_{max} = 1/0.0019 = 526.32 \mu\text{mol/L min}$ and $K_m = 0.2875/0.0019 = 151.32 \mu\text{M}$. In this case, the parameters are already more real. However, if we eliminate a third point, the results seem better, since now the points are distributed throughout the graph. Figure 5 shows this last plot.

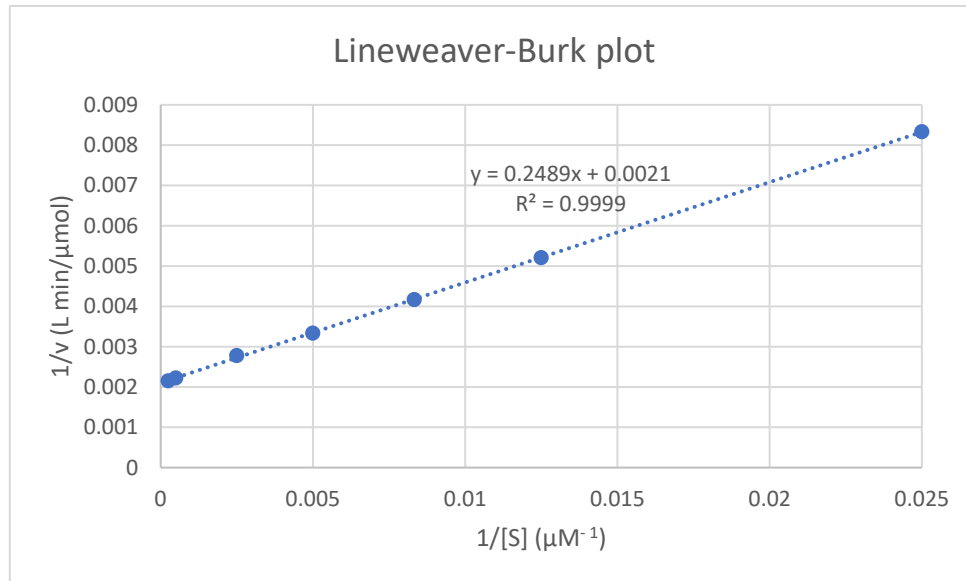


Figure 5. Lineweaver-Burk Plot ($1/v$ Versus $1/[S]$). In This Graph, the Points (5, 1.23), (0.25, 0.067), (0.05, 0.0167) Have Been Removed. These Points to (0.2, 0.81), (4.0, 15), (20, 60), the Lowers $[S]$ and Lowers v .

The kinetic parameters calculated by removing three points were: $V_{max} = 1/0.0021 = 476.19 \mu\text{mol/L min}$ and $K_m = 0.2489/0.0021 = 118.52 \mu\text{M}$.

Calculation of the Kinetic Parameters from Eadie-Hofstee Plot Using Linear Regression

This type of linear regression is obtained by multiplying the Lineweaver-Burk equation by $v \cdot V_{max}$. Rearranging the equation, we obtain:

$$v = -K_m (v/[S]) + V_{max}$$

The representation of v versus $(v/[S])$ shows a line, whose slope is directly $-K_m$ and its intersection is V_{max} . In addition, since the slope is negative, the graph is limited to the space between the two axes, which means that the points are in a limited area. Figure 6 shows this representation.

Although in the graph of Figure 6 there is a point that does not fit the line, even if this point is removed, the values of the graph are not affected too much. The following values of the kinetic parameters are obtained: $K_m = 122.51 \mu\text{M}$ and $V_{max} = 476.83 \mu\text{mol/L min}$. If the point of $v/[S] = 3 \mu\text{M}$ and $v = 60 \mu\text{mol/L min}$ (which is the one outside the line, with $[S] = 20 \mu\text{M}$) is removed, the values obtained are: $K_m = 119.51 \mu\text{M}$ and $V_{max} = 476.34 \mu\text{mol/L min}$. These kinetic parameters are very similar to those obtained without removing this point. It is not necessary

to remove any point to obtain correct values of kinetic constants, and also, the points are distributed along the line.

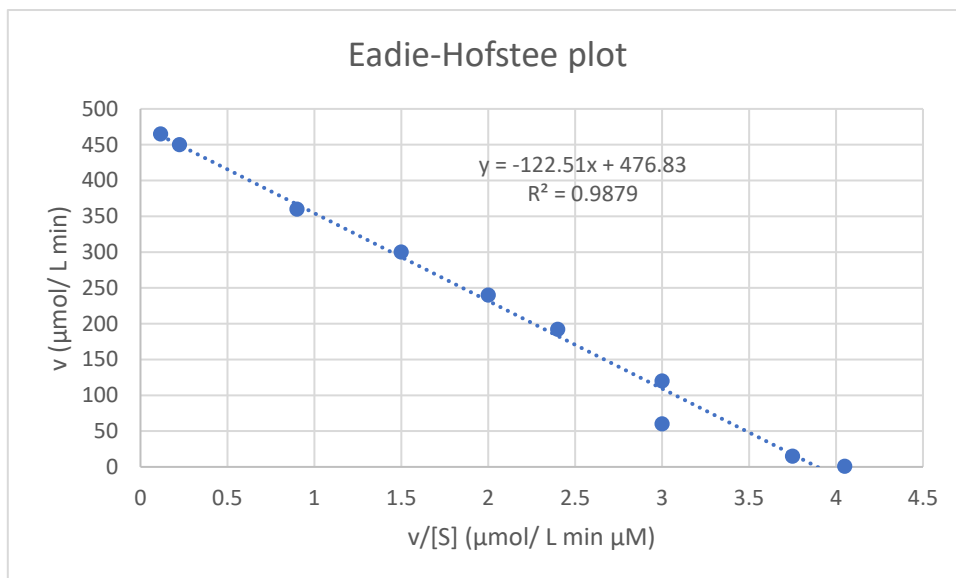


Figure 6. Eadie-Hofstee Plot ((v) Versus (v/[S])). This Plot Shows All the data for the Problem.

Calculation of the Kinetic Parameters from Hanes-Woolf Plot Using Linear Regression.

The Hanes-Woolf equation is obtained by multiplying the Lineweaver-Burk equation by [S]:

$$[S]/v = (1/V_{max}) [S] + (K_m/V_{max}).$$

The representation of [S]/v versus [S] shows the line in Figure 7, where the slope of the line is (1/V_{max}) and the intersection is (K_m/V_{max}).

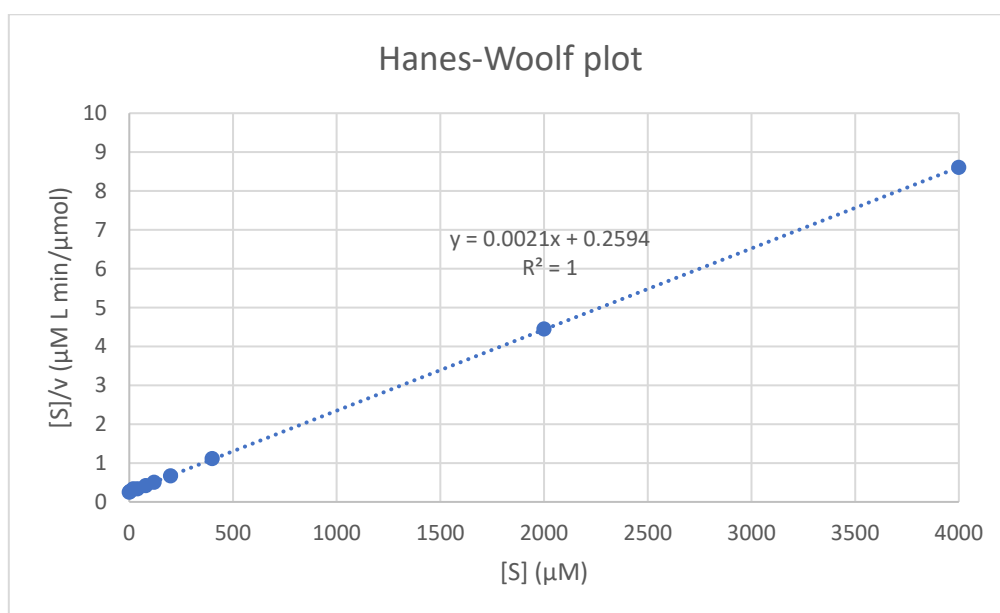


Figure 7. Hanes-Woolf Plot (([S]/v) Versus ([S])). This Plot Shows All the Data for the Problem.

The Hanes-Woolf plot has a positive slope, just like the Lineweaver-Burk plot. But in this case, unlike the Lineweaver-Burk plot, the points on the right of the graph are those with higher [S], which do not have as much error as those on the left of the plot, with lower [S]. Although these points are more separated from the others, as they have a lower error, the parameters obtained are not so much affected if the points are removed. The values of the kinetic constants for the line in Figure 7 are: $V_{max} = 1/0.0021 = 476.19 \mu\text{mol/L min}$ and $K_m = 0.2594/0.0021 = 123.52 \mu\text{M}$. When removing the point on the right of Figure 7 (4000, 8.60), corresponding to $[S] = 4000 \mu\text{M}$ and $v = 465 \mu\text{mol/L min}$, the values of the kinetic parameters obtained are: $V_{max} = 1/0.0021 = 476.19 \mu\text{mol/L min}$ and $K_m = 0.2594/0.0021 = 122.86 \mu\text{M}$, very similar to the previous data calculated.

Calculation of the Kinetic Parameters Using a Non-Linear Regression.

A non-linear regression is the most accurate method to obtain the kinetic parameters. On the Internet there are several web pages that allow a non-linear regression for the Michaelis-Menten equation. One of these web pages is designed exclusively for Michaelis-Menten kinetics [Herraez, 2021], and it is not necessary to introduce the equation to fit. Entering the data from Table 1 on this web page, the parameter obtained were: $V_{max} = 477 \pm 3 \mu\text{mol/L min}$ and $K_m = 121 \pm 3 \mu\text{M}$. Table 2 shows a summary of the results obtained by the different methods hereby presented.

Table 2. Comparison of the Kinetic Parameters Obtained Using the Various Methods.

Method	V_{max} ($\mu\text{mol/L min}$)	K_m (μM)
Michaelis-Menten plot	480	120
	500	133.33
Lineweaver-Burk plot	370.37	91.26
([S] = 0.2 removed)	454.54	117.64
([S] = 0.2 and 4.0 removed)	526.32	151.32
([S] = 0.2, 4.0 and 20 removed)	476.19	118.52
Eadie-Hofstee plot	476.83	122.51
([S] = 3 removed)	476.34	119.51
Hanes-Woolf plot	476.19	123.52
([S] = 4000 removed)	476.19	122.86
Non-linear regression	477 ± 3	121 ± 3

Discussion

Non-linear regression is the most accurate method to calculate the kinetic parameters. The results shown in Table 2 indicate that the V_{max} varies between 474 and 480 $\mu\text{mol/L min}$, while the K_m varies between 118 and 124 μM . The Michaelis-Menten method is a very inaccurate method since a value of V_{max} equal to or greater than 465 $\mu\text{mol/L min}$ must be chosen. If a value from 466 $\mu\text{mol/L min}$ to 473 $\mu\text{mol/L min}$ or a value higher than 481 $\mu\text{mol/L min}$ is taken, the V_{max} values would be erroneous. On the other hand, the calculation of the K_m will depend on the values of [S] that we have in the zone of $v = V_{max}/2$. Furthermore, when calculating the K_m by interpolation

we have assumed that, in the zone close to $v = V_{\max}/2$, the points follow a linear line, but this is not the case since the plot is hyperbolic. Thus, although $V_{\max} = 500 \mu\text{mol/L min}$ is taken, the K_m obtained by interpolation to a straight line is not, since $K_m = 133.33 \mu\text{M}$ is not in the interval of the values obtained by non-linear regression. From the Lineweaver-Burk graph, for this problem, the first 3 points had to be removed to obtain a correct value of V_{\max} . It is evident that the low $[S]$ can have large errors, which is what happened in this proposed problem. The Eadie-Hofstee and Hanes-Woolf plots are both good in order to obtain the correct kinetic parameters.

In the case of the Eadie-Hofstee plot, the values of the kinetic parameters are obtained directly, from the slope and the intersection of the line. However, the Hanes-Woolf plot does not directly generate the kinetic parameters. In this last graph it is also observed, as in the Lineweaver-Burk graph, that the points are not distributed along the line. However, the points that will influence the lineal regression are those with the highest $[S]$ (Figure 7), which have smaller errors. The lowest $[S]$ points, which can be the wrong ones, are all accumulated to the left of the graph, and other more exact points can compensate their errors. After performing the problem in the computer lab classes, the students understand clearly the name of each of the graphs, as well as which plot generates better values when calculating the kinetic parameters. Students can also understand how they should operate to obtain the kinetic parameters by means of a non-linear regression method.

Conclusion

Michaelis-Menten graph does not allow an exact calculation of the parameters, since it depends on the value that we decide to give to V_{\max} . This value is improvised, and K_m values are calculated depending on it, and thus they can be very different depending on which V_{\max} is taken. With all the data in the problem, the Lineweaver-Burk method is the most inaccurate, as errors in the low $[S]$ can lead to miscalculations of the parameters. The linear methods that generate the best results are those obtained with the Eadie-Hofstee and Hanes-Woolf graphs. However, the Eadie-Hofstee plot directly determines the parameters from the slope and the intersection of the line. For this reason, the Eadie-Hofstee graph is the most used in scientific articles on enzyme kinetics.

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Author Information


Josep J. Centelles

 <https://orcid.org/0000-0002-6289-9678>

Departament de Bioquímica i Biomedicina Molecular, Facultat de Biologia, Universitat de Barcelona, Avda. Diagonal 643, 08028-Barcelona Spain


Contact e-mail: josepcentelles@ub.edu

Estefania Moreno

 <https://orcid.org/0000-0002-2491-5753>


Departament de Bioquímica i Biomedicina Molecular, Facultat de Biologia, Universitat de Barcelona, Avda. Diagonal 643, 08028-Barcelona Spain

Pedro R. de Atauri

 <https://orcid.org/0000-0002-7754-7851>

Departament de Bioquímica i Biomedicina Molecular, Facultat de Biologia, Universitat de Barcelona, Avda. Diagonal 643, 08028-Barcelona Spain

Santiago Imperial

 <https://orcid.org/0000-0001-8749-1428>

Departament de Bioquímica i Biomedicina Molecular, Facultat de Biologia, Universitat de Barcelona, Avda. Diagonal 643, 08028-Barcelona Spain
